### 3.1 The Ideal Diode (pp.139-141)

A. The Ideal Diode Symbol

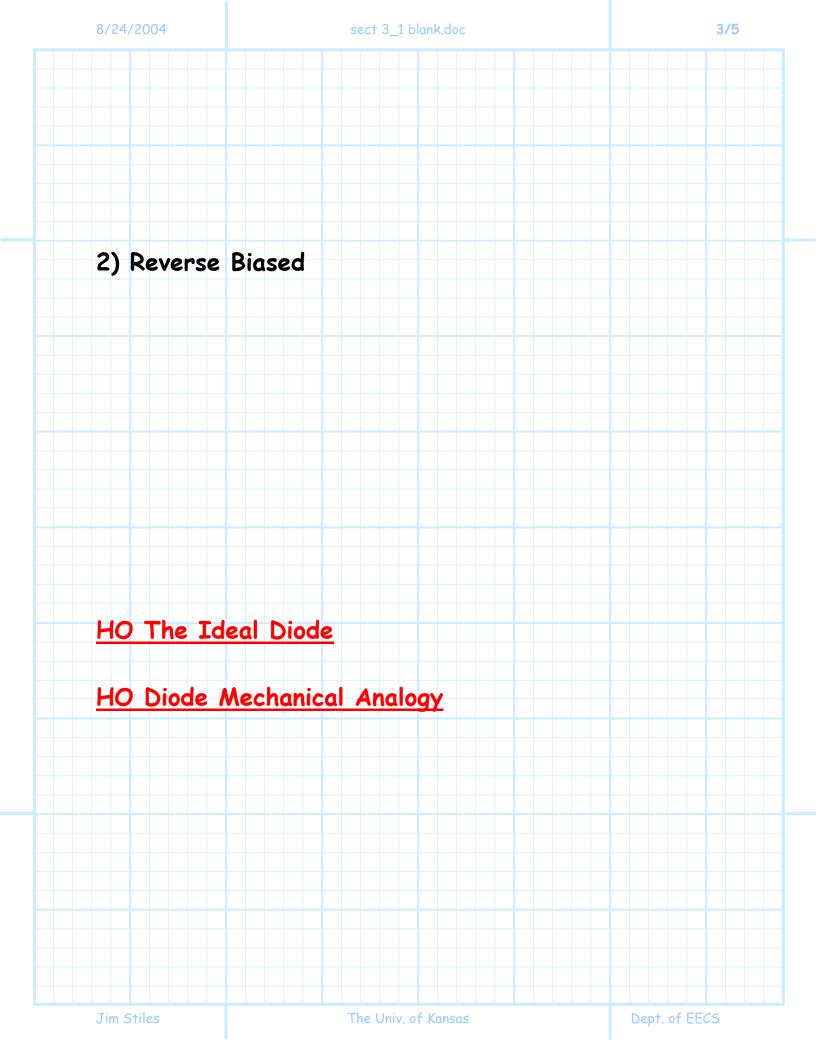
B. Ideal Diode Behavior

1/D 1

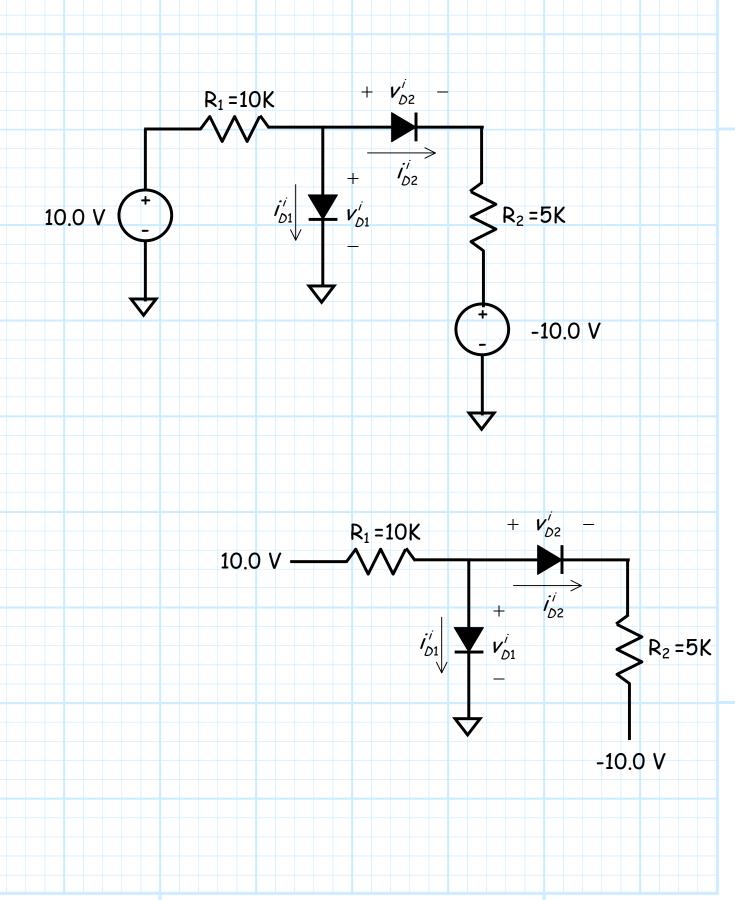


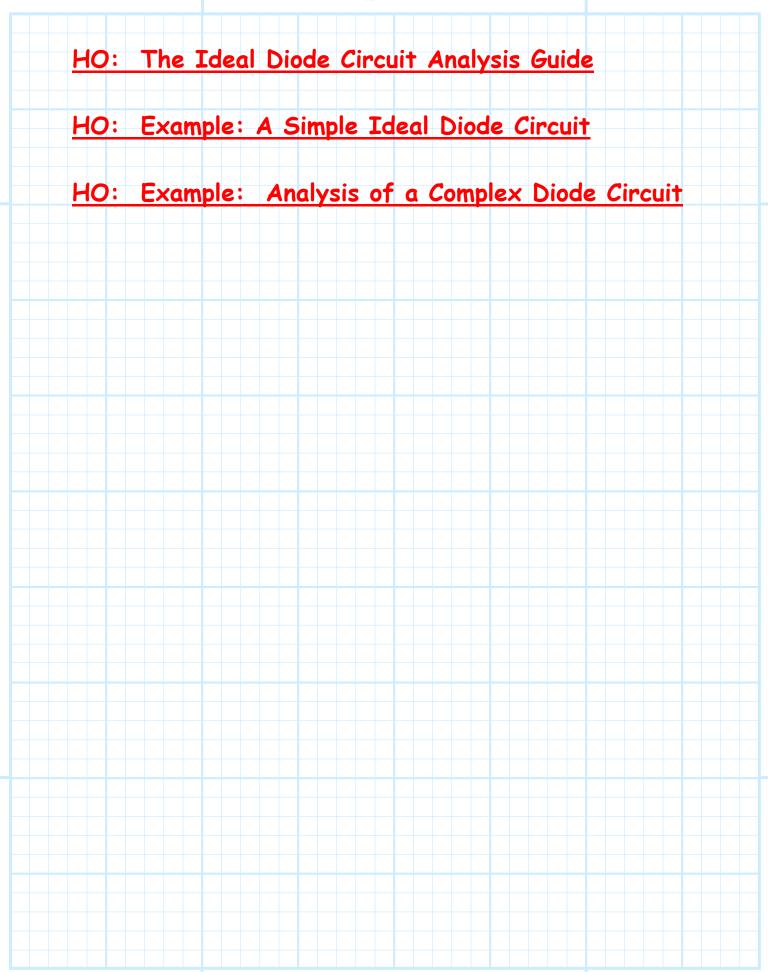
C. Diode Bias Regions

1) Forward Biased



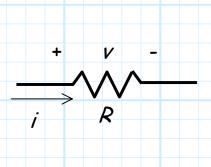
### D. Ideal Diode Circuit Analysis



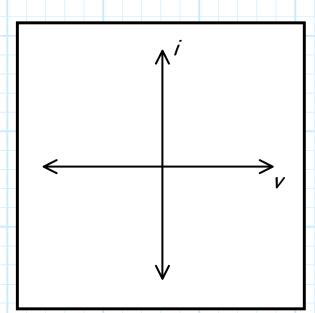


### Linear Device Behavior

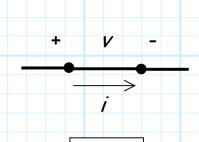
1) Recall the circuit behavior of a resistor:



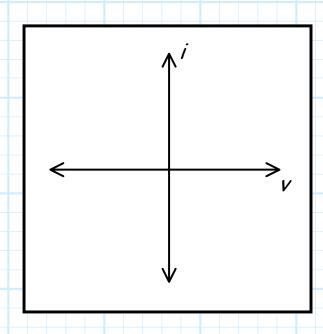
$$i = \frac{v}{R}$$



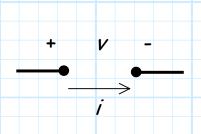
2) If R=0, then we have a short circuit:

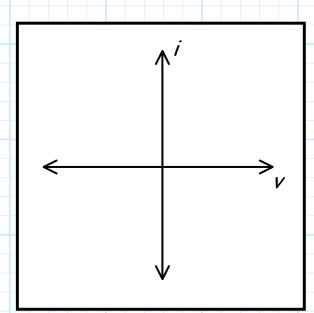


$$v = 0$$

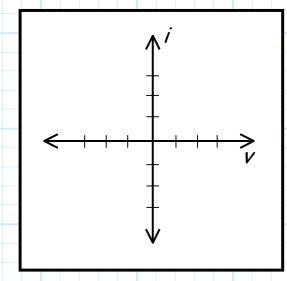


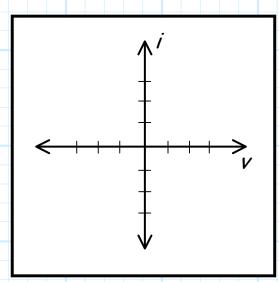
3) If  $R=\infty$ , then we have a **open** circuit:

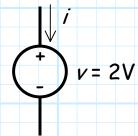




4) We can also plot the behavior of both current and voltage sources:



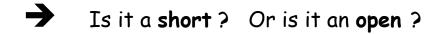


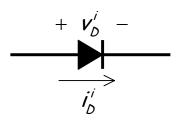


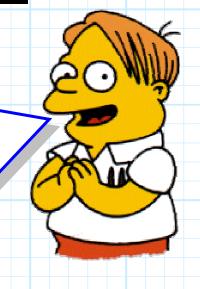
*i* = 1 A  $\bigvee_{-1}^{+1}$ 

## The Ideal Diode

An ideal diode—the circuit device with a split personality!







	$V_D^i < 0$	$V_D^i = 0$	$V_D^i > 0$
$i_D^i > 0$	invalid	forward biased	invalid
$i_D^i = 0$	reverse biased	no bias	invalid
$i_D^i < 0$	invalid	invalid	invalid

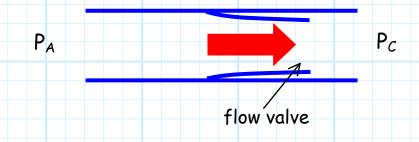
# The Diode Mechanical Analogy

An ideal diode is sort of like a mechanical valve!

side liquid side C

flow valve

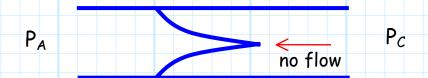
<u>Case 1:</u> Valve allows liquid to flow in pipe from side A to side C.



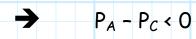
There is no drop in pressure (P) from side A to side C.

$$\rightarrow$$
  $P_A - P_C = 0$ 

### <u>Case 2</u>: Valve prevents liquid from flowing back from side C to side A.



No flow occurs when pressure  $P_c$  is greater than pressure  $P_A$ 



#### Note the analogies with an ideal diode:

#### Valve

Pressure

Liquid Flow

Side A

Side C

Case 1

Case 2

#### Diode

Voltage

Current

Anode

Cathode

Forward Bias

Reverse Bias

# The Ideal Diode Circuit Analysis Guide

Follow these easy steps to successfully analyze a circuit containing one or more ideal diodes!

Step 1: ASSUME a bias state for each ideal diode.

⇒ In other words, GUESS!!

Either,

- a) ASSUME an ideal diode is forward biased, or
- b) ASSUME it is reversed biased.

<u>Step 2:</u> ENFORCE the equality condition consistent with your assumption.

a) If you assume an ideal diode is **f.b.**, then *ENFORCE* the equality:

 $v_D^i = 0$ 

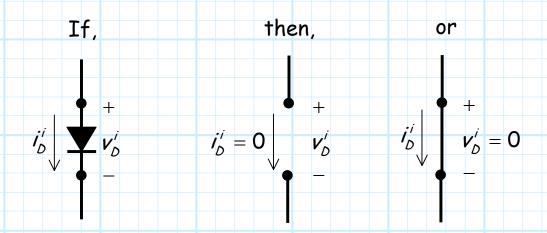
HOW?  $\Rightarrow$  By replacing the ideal diode with a short circuit!

b) If you assumed an ideal diode was r.b., then ENFORCE the condition that:

 $i_{\mathcal{D}}^{i}=0$ 

HOW?  $\Rightarrow$  By replacing the ideal diode with an open circuit.

IMPORTANT !!! Retain the same current and voltage definitions when you replace the ideal diode!



Step 3: ANALYZE the circuit.

After the all ideal diodes have been replaced with either shorts or opens:

- a) Determine all desired (required) circuit values.
- b) Determine  $i_D^i$  through each **short** circuit and  $v_D^i$  across each **open** circuit.

Step 4: CHECK the inequality consistent with your assumption to see if this assumption is correct.

HOW 22

a) An ideal diode cannot have negative current flowing through it. If you ASSUMED the ideal diode was forward biased, CHECK to see if the short circuit current is positive, i.e.:

 $i_D^i > 0$ 

If true, you ASSUMED correctly! If not, your f.b. assumption is wrong.

b) An ideal diode cannot have positive voltage across it. If you ASSUMED the ideal diode was reversed biased, CHECK to see if the open circuit voltage is negative, i.e.:

 $V_D^i < 0$ 

If true, you ASSUMED correctly! If not, your r.b. assumption is wrong.

Step 5: If you ASSUMED incorrectly, then change your assumptions and return to step 1!

#### Notes on ideal diode circuit analysis:

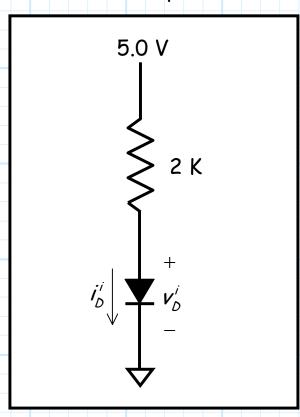
1) You must check all assumptions in this form:

$$i_{D}^{i} = 2 \, mA > 0 \, \checkmark \quad \text{or} \quad V_{D}^{i} = 2.2 > 0 \, X$$

- 2) Do not check the condition that you enforced!
- 3) For every circuit, one and only one assumption will be valid.

## Example: A Simple Ideal Diode Circuit

Consider this simple circuit that includes an ideal diode:



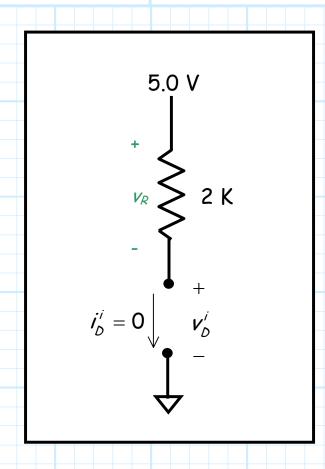
Q: What are  $i_D^i$  and  $v_D^i$ ?

A: Follow the five easy analysis steps!

Step 1: Let's ASSUME the ideal diode is reverse biased (we're just guessing!).

**Step 2:** We therefore *ENFORCE*  $i_D^{\prime} = 0$  by replacing the ideal diode with an **open** circuit.

**Step 3:** Now we ANALYZE the circuit; finding the value of  $V_D^i$ .

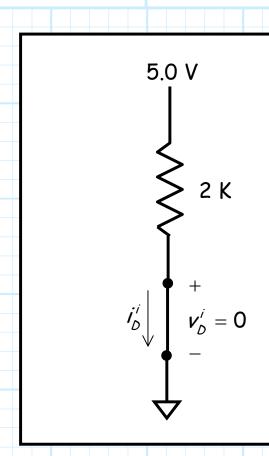


**Step 4:** Now let's CHECK our result.  $\Rightarrow$  **Is**  $V_D^i < 0$ ??

$$V_{\mathcal{D}}^{i} =$$

We must change our assumption, and then start over (Doh!).

- 1) Now ASSUME the ideal diode is forward biased (what's left?).
- 2) We therefore *ENFORCE*  $v_D^i = 0$  by replacing the ideal diode with an **short** circuit.
- 3) Now we ANALYZE the circuit; finding the value of  $i_{D}^{i}$ .



KVL:

4) Now, let's CHECK our result.  $\Rightarrow$  Is  $i_D^i > 0$ ??

$$i_D^i =$$

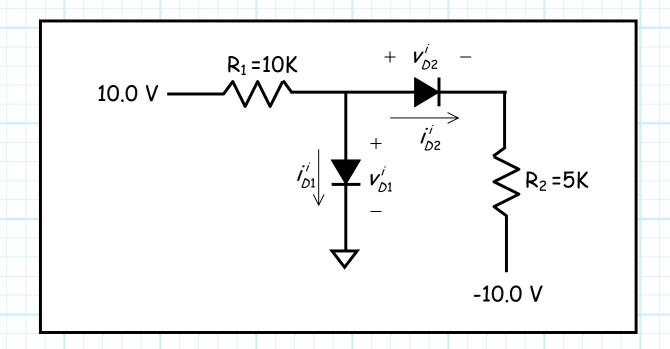
Our assumption is correct!

Therefore, in this circuit, we now know that:

$$v_{\mathcal{D}}^{i} = 0$$
 and  $i_{\mathcal{D}}^{i} =$ 

## Example: Analysis of a Complex Diode Circuit

Consider this circuit with two ideal diodes:



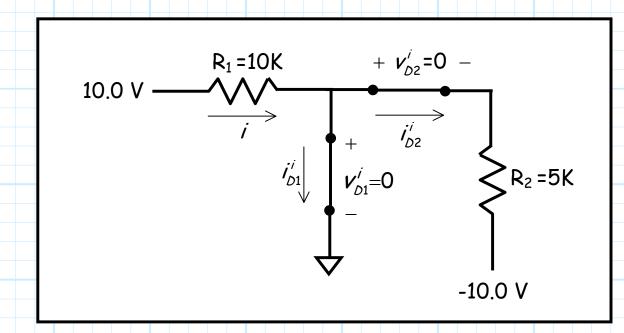
Let's analyze this circuit and find  $v_{D1}^i$ ,  $i_{D1}^i$ ,  $v_{D2}^i$ , and  $i_{D2}^i$ !

Remember, we must accomplish each of the five steps:

Step 1: ASSUME that both  $D_1$  and  $D_2$  are "on" (might as well!).

**Step 2:** ENFORCE the equalities  $v_{D1}^{i} = 0 = v_{D2}^{i}$ , by replacing each ideal diode with a short circuit.

**Step 3:** ANALYZE the resulting circuit, and find  $i'_{D1}$  and  $i'_{D2}$ .



Begin with KCL:

$$\dot{i}=\dot{i}_{D1}^{\prime}+\dot{i}_{D2}^{\prime}$$

where

and

$$i_{D2}^{i} =$$

Therefore,  $i_{D1}^{i} =$ 

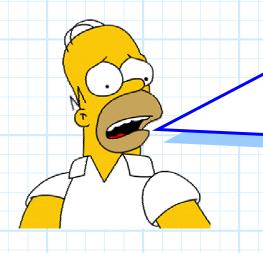
$$i_{D1}^{i} =$$

Step 4: Now we must CHECK inequalities to see if our assumptions are correct!

$$i_{D1}^{i} =$$

$$i_{D2}^{'} =$$

One assumption is therefore **INCORRECT**. We must proceed to step 5—change our assumptions and completely start again!



Q: Wait a second! We don't have to completely start from the beginning, do we? After all, our assumption about diode  $D_2$  turned out to be true—so we already know that  $i_{D2}^i = 0$ , right?

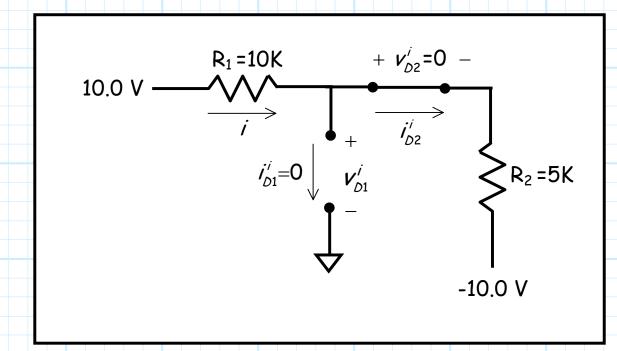
**A:** NO! The solution for diode  $D_2$  is dependent on the state of both diodes  $D_1$  and  $D_2$ . If the assumption of just **one** diode turns out to be incorrect, then the solutions for **all** diodes are **wrong**!

So, let's change our assumption and start all over again!

Step 1: Now ASSUME that  $D_1$  is "off" and  $D_2$  is "on".

Step 2: ENFORCE  $i_{D1}^{i} = 0$  ( $D_1$  open) and  $V_{D2}^{i} = 0$  ( $D_2$  short).

**Step 3:** ANALYZE resulting circuit, and find  $v_{D1}^{i}$  and  $i_{D2}^{i}$ .



Note  $i = i_{D2}^i =$ 

and from KVL:

4) CHECK our assumptions.

$$i_{D2}^{i} =$$

$$V_{D1}^{i} =$$

:. Assumptions are correct! We are finished!



$${m V}_{{\cal D}1}^i =$$

$$i_{D1}^{i}=0$$

$$V_{D2}^{i}=0$$

$$i_{D2}^{i} =$$